

2023.09.25

EC4301

hw#4 (Due by Oct. 11)

Let  $E_j(t, f) = E_0 e^{if_j t}$  be a monochromatic wave, where  $E_0 = 1$  and  $f_0 = 10^{14}$  Hz.

Let the frequency range be  $-\Delta < \delta f < \Delta$ , where  $\Delta = 0.1f_0$ . Thus,  $f_j = f_0 + \delta f$ .

(a) Plot  $E_j(t, f)$  for  $t$  and  $\delta f$ , where  $-100T < t < 100T$  and  $T = f_0^{-1}$ .

(b) Plot mean intensity  $\langle I(t) \rangle = E(t)E(t)^*$ , where  $E(t) = \frac{1}{(2N+1)} \sum_{f=-\Delta}^{\Delta} E_j(t, f)$ . Here,  $2N+1$  represents total frequency divisions. Here  $E(t)$  represents the frequency sum of  $E_j$  for all  $f_j$  at each  $t$ .

(c) (Bonus) Apply weighted factors of Gaussian distribution to  $E_j(t, f)$ . Use the following Gaussian function  $g1$ :

$g1(x) = e^{-\left(\frac{x-b}{c\sqrt{2}}\right)^2}$ , where  $b=0$  and  $c=5$ . Here,  $b(x)$  represents  $f_0$  (frequency detuning  $\delta f$ ). The  $c$  represents the standard deviation of the bandwidth. Hint:  $E_j(t, f) \rightarrow E_j(t, f_j) * g1(f_j)$ .